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ALGORITHMS FOR GENERATING A SKEW-T, LOG P DIAGRAM AND COMPUTING SELECTED METEOROLOGICAL QUANTITIES

G. S. Stipanuk

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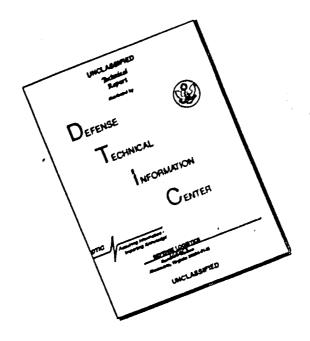
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ALGORITHMS FOR GENERATING A SKEW-T, log p DIAGRAM AND COMPUTING SELECTED METEOROLOGICAL QUANTITIES

By

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	Algorithms						
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CONTENTS

F	age
SYMBOLS	3
INTRODUCTION	5
THE SKEW-T, log p DIAGRAM	5
ALGORITHMS FOR SELECTED METEOROLOGICAL QUANTITIES	12
Mixing Ratio: W	12 12
Saturation Vapor Pressure: E	12
Actual Vapor Pressure: EA	13
Potential Temperature: 8	13
The Wet Bulb Temperature and Wet Bulb Potential Temperature: TW, 0W	13
Potential Temperature: TPW, 0PW	14
	14
The Psuedo Equivalent Temperature: TE	
Thickness of a Layer: Z	15
The Lifting Condensation Level: LCL	
	16 17
The Convective Temperature: Cl	1/
APPLICATIONS	18
LITERATURE CITED	21
BIBLIOGRAPHY	22
APPENDIX A - PROGRAM LISTING	24

SYMBOLS

- CCL Convective condensation level
- Cp Heat capacity of air at constant pressure
- CT Convective temperature
- E Actual vapor pressure
- ES Saturation vapor pressure
- FR Relative humidity
- i,j,k indexes
- L Latent heat of vaporization of water
- LCL Lifting condensation level
- M Saturation vapor pressure over water
- P Pressure
- P* Pressure correction
- PB Pressure at the bottom of a layer
- PC Pressure at the convective condensation level
- PI Pressure at the intersection
- PM Pressure at the top of the mixing layer
- PS Surface pressure
- PT Pressure at the top of a layer
- R Gas constant
- T Temperature
- T* Temperature correction
- TD Dewpoint temperature
- TDS Dewpoint temperature at the surface

Preceding page blank

 T_{DA} - Temperature on a dry adiabatic curve

TE - Psuedo equivalent temperature

TI - Temperature at an intersection

 $T_{\rm M}$ - Temperature at the top of the mixing layer

T - Temperature on a mixing ratio curve

T_{SA} - Temperature on a saturation adiabat curve

TW - Wet bulb temperature

W - Mixing ratio

W - Mean mixing ratio

X - Coordinate

Y - Coordinate

Z - Thickness of a layer

0 - Potential temperature

θE - Equivalent potential temperature

 θ_{ς} - Parameter for saturation adiabat

INTRODUCTION

The increasing availability of computing facilities, programmable calculators, and minicomputers allows many of the computations currently performed by manual graphics to be done by computer. This paper discusses numerical methods of computing meteorological quantities which are usually manually derived from analysis on a SKEW-T, log p DIAGRAM (or SKEW-T). The numerical methods used were selected for their simplicity and accuracy. A mathematical characterization of the SKEW-T and algorithms for computing several meteorological quantities are presented. Finally, a discussion of the application of these methods and a FORTRAN program listing to accomplish the computations are included.

THE SKEW-T, log p DIAGRAM

The SKEW-T, log p DIAGRAM [I] is a thermodynamic chart with five families of curves, five types of scales, and three data blocks. Various numerical information is also tabulated on the SKEW-T. This paper is concerned chiefly with the five families of curves which are associated with pressure, temperature, dry adiabat, saturation adiabat, and mixing ratio.

The first two families of curves, temperature and pressure, are used to locate points on the chart. An arbitrary coordinate system has been selected to measure distances. Let the origin correspond to the point at a temperature of OC (centigrade) and a pressure of 1000 mb (millibars). Take the X direction to be parallel to the pressure lines (horizontal), with positive X to the right. The point at a temperature of IC and a pressure of 1000 mb is on the positive side of the origin. The Y direction is perpendicular to the X direction. Positive Y is towards lower pressures (up). A point on the chart which is specified by its temperature and pressure may be transformed to X,Y coordinates by Eqs. (1) and (2). The components in the X,Y coordinate system are given in inches.

$$X = .1408T - 10.53975 \log_{10} P + 31.61923$$
 (1)

$$Y = -11.5 \log_{10} P + 34.5$$
 (2)

The X,Y coordinates have been scaled to USAF SKEW-T, log p DIAGRAM DOD-WPC-9-16-1. See [1].

The remaining three families of curves, TMR, TSA, and TDA, are given in Table I. The temperatures are specified as a function of pressure and a parameter, the parameter serving as a means of specifying a particular curve of the family.

The temperature T at an arbitrary pressure on a saturation adiabat is determined by the bisection method.† The temperature is assumed to lie in the range -80C to 40C. An initial guess of -20C is made and the correction, T*, computed. The correction term decreases by a factor of 1/2 after each correction. Terminating after 13 corrections gave satisfactory results. The algorithm for computing the temperature on a saturation adiabat is based on Eq. (3):

$$\theta = (\theta E) \cdot EXP(-\frac{L \cdot W}{Cp \cdot T})$$
 (3)

The latent heat of vaporization L and the heat capacity of air at constant pressure Cp, are considered constant. Since it is not known how accurately the saturation adiabat could be determined from Eq. (3), Table 2 was constructed using List [2] as a standard. The temperature on an arbitrary mixing ratio curve W is computed by first computing the saturation vapor pressure M. An approximation to the inverse saturation vapor pressure function is then used to compute the temperature.

In addition to the algorithms which generate the curves for each family, it is necessary to have algorithms which determine which curve in a family passes through an arbitrary point (T,P). Algorithms to accomplish this are given in Table 3.

The bisection method is a numerical technique which decreases the difference between the upper and lower estimates by a factor of 1/2 per iteration.

SKEW-T ALCORITHMS

	ALGORI THM	Intial $T_{DA}(\theta, P) = \theta(\frac{P}{1000}) \cdot 285$. T is in Kelvin. K=C + 273.16 $ T_{MR}(W,P) = 10^{(alog_{\parallel}0^m + b)} + c + d(m^f + g)^2 $	a = .0498646455	b = 2,4082965	c = 280.23475	d = 38.9114	f = .0915	
PADANETED	LANAIME I E.	0 potential temperature	W mixing rat						
FAMILY	1 7 11 1 1	Dry Adiabat	Mixing Ratio						

FAMI LY	PARAMETER	ALGORITHM
Saturation Adiabat	e the temperature at 1000 mb	$T_{SA}(\theta_{S},P) = T_{1} + \sum_{i=1}^{12} T_{i}^{*}$
		$T_{i} = 253.16 \text{ K}$ $T_{i}^{*} = \frac{120}{2^{i}} \text{ SIGN} \left[a \text{ EXP} \left\{ \frac{bW(T_{i}, P)}{T_{i}} \right\} - T_{i} \frac{(1000) \cdot 288}{P} \right]$
		T = T + T* T = T = T = T = T = T = T = T = T =
		b = -2.6518986
		$W(T,P) = \frac{622 \text{ ESAT (T)}}{P - \text{ESAT (T)}}$
		ESAT (T) = 10.**(23.832241-5.02808*ALOG10(T)-1.3816E-7* 10.**(11.344-0.0303998*T)+8.1328E-3*10.** (3.49149-1302.8844/T)-2949.076/T)
		NOTE: T is in Kelvin. K = C + 273.16 ESAT is from Nordquist [3].
		The SIGN function is -1 or 1 wrresponding

to the algebraic sign of the argument.

TABLE 2

TEMPERATURE AND ERROR ON SELECTED SATURATION ADIABATS AT SELECTED PRESSURES

Pressure (mb)	Temperature (C)	Error (C)
(IIIO)	(6)	(6)
1000.0	40.0000	
70:.5	29.9877	.0122
490.7	19.9536	.0463
344.7	9.9194	.0805
245.4	1733	1733
179.6	-10.2221	2221
000.0	30.0000	
733.0	19.9829	.0170
544.0	9.9633	.0366
412.4	0561	0561
321.4	-10.0756	0756
257.7	-20.1538	1538
212.0	-30.2612	2612
177.6	-40.3247	3247
0.000	20.0000	
770.0	9.9780	.0219
606.0	 0561 ·	0561
489.0	-10.0463	0463
403.0	-20.1245	- 1245
338.0	-30.1879	1879
286.4	-40.2368	2368
243.5	-50.2709	2709
206.8	-60.2612 -70.2661	2612
174.7	-70.2001	2661
000.0	10.0000	
805.0	0415	0415
663.0	-9.9877	.0122
554.0	-20.0952	0952
470.0	-30.0268	0268
400.0	-40.1196	1196
341.0	-50.1538	1538
289.9	-60.1586	1586
245.1	-70.1489	1489
205.7	-80.1098 -90.1147	1098 1147
171.0	-30.1147	1147

TABLE 2 (con.)

Pressure (mb)	Temperature (C)	Error (C)
0.000	.0000	
833.0	-9.9731	.0268
703.0	-19.9926	.0073
599.0	-29.9829	.0170
511.0	-40.1196	1196
436.4	-50.1391	1391
371.3	-60.1293	1293
314.0	-70.1196	1196
263.5	-80.0952	0952
219.1	-90.0854	0854
1000.0	-10.0000	
849.0	-20.0073	0073
726.0	-29.9829	.0170
621.0	-40.0756	0756
531.2	-50.0512	0512
452.2	-60.0415	0415
382.4	-70.0463	0463
266.9	-89.9975	0024
0.000	-20.0000	
856.8	-30.0!22	0122
734.8	-40.0170	0170
628.c	-50.0366	0366
535.3	-60.0268	0268
452.8	-70.0170	0170
380.0	-80.0073	0073
316.0	-89.9829	.0170

TABLE 3

DETERMINING A CURVE THROUGH A GIVEN POINT

FAMILY PARAMETER FOR CURVE PASSING THROUGH (T,P)

Dry Adiabat

$$\theta = T(\frac{1000}{P}) \cdot 288$$

Mixing Ratio

$$W = \frac{622 \text{ ESAT(T)}}{P - \text{ ESAT(T)}}$$

Saturation Adiabat

$$\theta_{S} = \frac{T(\frac{1000}{P}) \cdot 288}{EXP(\frac{bW(T,P)}{T})}$$

$$b = -2.6518986$$

NOTE: T is in Kelvin. K = C + 273.16 (see Table I for a definition of ESAT)

ALGORITHMS FOR SELECTED METEOROLOGICAL QUANTITIES

Several meteorological quantities which are usually manually derived from an analysis of a SKEW-T were selected for discussion. Algorithms are presented for computing these meteorological quantities. The selection of symbols is somewhat different than is customary because of current symbol limitations on computers. But by referring to the List of Symbols, the reader will have no difficulty. Units are the same as those used on the SKEW-T [1].

Mixing Ratio: W

The mixing ratio W is computed from the pressure P and the dewpoint temperature TD by using the function ESAT, which is defined in Table 1.

$$W = \frac{622 \text{ ESAT(TD)}}{P - \text{ ESAT(TD)}} \tag{4}$$

TD is in degrees Kelvin, the pressure P in millibars, and W in grams of water vapor per kilogram of dry air. The <u>saturation</u> mixing ratio is obtained by using the dry bulb temperature in place of the dewpoint temperature.

Relative Humidity: FR

The relative humidity is computed from the temperature T and the dewpoint temperature TD by using ESAT. Both T and TD are in degrees Kelvin.

$$FR = 100 (ESAT(TD)/ESAT(T))$$
 (5)

Saturation Vapor Pressure: ES

ESAT gives the saturation vapor pressure in millibars from the dry bulb temperature T, which is in degrees Kelvin.

$$ES = ESAT(T)$$
 (6)

Actual Vapor Pressure: E

The dewpoint temperature TD is used in place of T in Eq. (6).

Potential Temperature: 0

The potential temperature is computed from the dry bulb temperature T in Kelvin and the pressure P in millibars.

$$\theta = T \left(\frac{1000}{P}\right)^{288}$$
 (7)

The Wet Bulb Temperature and Wet Bulb Potential Temperature: TW,0W

The wet bulb temperature is approximated by calculating the psuedo wet bulb temperature. The arguments are surface dewpoint temperature, surface temperature, and pressure, which are symbolized by TDS, TS, and PS, respectively. TDS and TS are in Kelvin, P in millibars. First a mixing ratio curve W, which passes through (TDS, PS), is determined. From Table 3 we have:

$$W = \frac{622 \text{ ESAT (TDS)}}{P - \text{ ESAT (TDS)}}$$
 (8)

Next a dry adiabat, which passes through (TS, PS), is determined. Again by referring to Table 3 we have:

$$\theta = TS(\frac{PS}{1000}) \cdot 288 \tag{9}$$

Two curves have now been specified: T_{MR} (W, P) and T_{DA} (0, P). The next step is to locate the pressure at which the curves intersect. This is done by an iterative procedure. An initial guess that the intersection pressure PI is equal to the surface pressure is made. A correction is computed and a revised guess made. When $(T_{MR} - T_{DA})^2$ is loss than .0001 degrees, the process is terminated.

$$PI_{l} = PS$$
 (10)

$$PI_{i} = PI_{i-1} + P*_{i-1}$$
 (11)

$$P_{k}^{*} = P_{k} 2^{(.02(T_{MR}(W,P_{k}) - T_{DA}(\theta,P_{k})))}$$
 (12)

It is found that six iterations were sufficient to compute PI to within I mb. Once the pressure and hence temperature at the intersection are known, a saturation adiabat through the intersection point (TI, PI) is found. Referring to Table 3 we have:

$$\theta_{S} = \frac{TI \frac{(1000) \cdot 288}{PI}}{EXP \frac{(bW(TI, PI)}{TI})}$$
(13)

Finally by following this saturation adiabat to the surface pressure PS and to 1000 mb, we get the wet bulb temperature TW and the wet bulb potential temperature θW , respectively.

$$TW = T_{SA} (\theta_S, PS)$$
 (14)

$$\theta W = T_{SA} (\theta_S, 1000)$$
 (15)

The Psuedo Wet Bulb Temperature and Pseudo Wet Bulb Potential Temperature: TPW, 0PW

Refer to the wet bulb temperature and wet bulb potential temperature above.

The Equivalent Potential Temperature: 0E

The equivalent potential temperature is computed from the same quantities used to compute the wet bulb temperature, i.e., the surface pressure, dewpoint temperature, and actual temperature. First compute the wet bulb temperature TW. The equivalent potential temperature can then be computed by the same process used to determine the parameter θ_S of a saturation adiabat through (TW, PS). Referring to Table 3 we have:

$$\theta E = \frac{TW}{EXP} \left(\frac{1000}{PS} \right)^{.288}$$

$$EXP \left(\frac{bW(TW, PS)}{TW} \right)$$
(16)

The Psuedo Equivalent Temperature: TE

First the equivalent potential temperature θE is computed. The psuedo equivalent temperature is then given by

$$TE = \theta E \left(\frac{PS}{1000}\right).288$$
 (17)

Thickness of a Layer: Z

It is assumed that the temperature and dewpoint temperature are known at N distinct, decreasing pressures. Thicknesses are computed in meters from the surface. The trapezoidal rule is used to integrate

$$Z = \frac{R}{.98} \int_{InPS}^{InPT} [T + .6078*W*T/(1000 + W)] d InP$$
 (18)

See Table I for a definition of W(T, P).

Rewriting Eq. (18) and noting that W<<1000 gives Eq. (19), which is used to perform the computation of Z:

$$Z = 29.2857 \left[\frac{(T_1 + T_2 + 6.078 \cdot 10^{-6} \cdot (W_1 \cdot T_1 + W_2 \cdot T_2))}{2} \cdot \ln(P_1/P_2) \right]$$

$$+ \frac{(T_2 + T_3 + 6.078 \cdot 10^{-6} \cdot (W_2 \cdot T_2 + W_3 \cdot T_3))}{2} \cdot \ln(P_2/P_3)$$

+ ... +
$$\frac{(T_n + T_{n+1} + 6.078 \cdot 10^{-6} \cdot (W_n \cdot T_n + W_{n+1} \cdot T_{n+1}))}{2} \cdot \ln(P_n/P_{n+1})$$
 (19)

The Lifting Condensation Level: LCL

The lifting condensation level is computed in the same manner that PI was computed for the wet bulb temperature. Eqs. (8), (9), (10), (11), and (12) are used. (T1, P1) locate the LCL.

The Convective Condensation Level: CCL

It is assumed that the temperature and dewpoint temperature are known at N distinct, decreasing pressures. The pressure at the top of the mixing layer PM must be greater than P_n , the last pressure level. Since PM is bounded by P_1 and P_n , there is a K such that

$$P_{k} > PM > P_{k+1} \tag{20}$$

First the mean mixing ratio, \overline{W} , in the P₁ - PM layer is computed:

$$\overline{W} = \frac{\sum_{i=1}^{K-1} \left[W(T_i, P_i) + W(T_{i+1}, P_{i+1}) \right] (InP_i - InP_{i+1})}{2(In P_i - In PM)}$$

$$+ \frac{\left[W(T_{k}, P_{k}) + W(T_{m}, PM)\right] (\ln P_{k} - \ln PM)}{2(\ln P_{l} - \ln PM)}$$
(21)

The intersection of T_{MR} (\overline{W} , P) and the curve defined by

$$T_{S}(P) = T_{k} - \frac{(T_{k+1} - T_{k})(InP - InP_{k})}{(InP_{k} - InP_{k+1})}$$
 (22)

(k is chosen such that P, > P > P,) defines the convective condensation level. This intersection can be found by first systematically comparing the difference between T_{MR} (W, P,) and T_{S} (P,) until the smallest i is found, such that

$$T_{MR}(\overline{W}, P_i) - T_S(P_i) < 0$$
 (23)

and

$$T_{MR}(\overline{W}, P_{i+1}) - T_{S}(P_{i+1}) > 0$$
 (24)

A bisection method is used to determine PC, the pressure at the CCL. An initial guess PC, is made, tested to see if $T_{MR}(\overline{W}, PC_1)$ equals $T_{S}(PC_1)$, and if not, corrected.

$$PC_{i} = .5 (P_{i} + P_{i+1})$$
 (25)

$$PC_{j} = PC_{j-1} + P*_{j-1} (corrector)$$
 (26)

$$P_{k}^{*} = \frac{(P_{i} + P_{i+1})}{2^{k}} SIGN (T_{MR} (\overline{W}, PC_{k}) - T_{S} (P_{k}))$$
 (27)

Ten corrections are made.

The Convective Temperature: CT

First the pressure PC at the convective condensation level is computed. The temperature at the CCL, TC, is computed from PC and \overline{W} :

$$TC = T_{MR} (\overline{W}, PC)$$
 (28)

A dry adiabat is determined.

$$\theta = TC \left(\frac{1000}{PC}\right).288$$
 (29)

Finally, the convective temperature CT is computed from θ and the surface pressure PS:

$$CT = \theta \left(\frac{PS}{1000} \right) \cdot 288$$
 (30)

APPLICATIONS

The algorithms are useful for data reduction purposes. The memory and speed requirements are not excessive and most computations can be carried out satisfactorily on a programmable calculator. In addition to data analysis, the algorithms are useful for generating backgrounds for the presentation of data. An example of a computer generated background and plotted sounding is given in Fig. 1. Computation of selected meteorological quantities from the sounding in Fig. 1 are presented in Table 4. A table of CCL temperatures, pressures, and heights was computed using an arbitrary decrement of -25 mb for the pressure at the top of the mixing ratio.

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Many individuals and groups contributed stimulating discussion and valuable time in assisting the author on this study and it is impossible to name them all. Deep appreciation is extended to the National Center for Atmospheric Research, which is sponsored by the National Science Foundation, for computer time used in this research. Mr. Walter S. Nordquist, who provided the impetus for this study, as well as many suggestions along the way and a critical reading of the manuscript, deserves much of the credit for this work. Finally, Mr. Alex Blomerth provided much administrative assistance, without which this study would have not been possible.

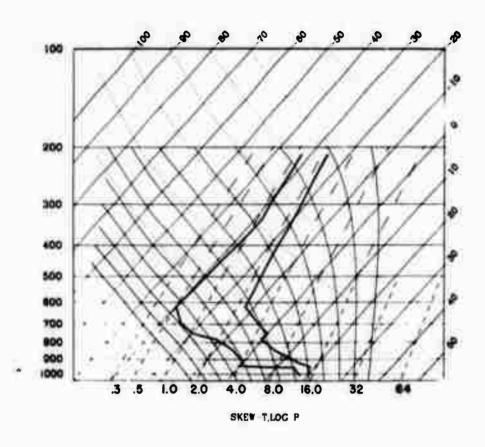


Figure I. A computer-generated SKEW-T background with a hypothetical profile of temperature and dewpoint temperature. Horizontal lines are pressure. Positive sloped lines are temperature (solid) and mixing ratio (dashed). Negative sloped curves are dry adiabat (dashed) and saturated adiabat (solid).

TABLE 4

AN EXAMPLE OF A VERTICAL SOUNDING

Press.	1013	953	050	042	020	0.47	777	745	601	600		210	-
	0		950	942	920	843	777	745	691	620	333	210	
Height		536	554	626	827	1553	2213	2549	3145	3984	8664	12047	
Pot. T.	19.3	22.3	23.3	23.2	21.3	19.8	19.8	24.0	24.5	26.2	74.1	115.0	
Temp.	20.4	18.2	19.0	18.2	14.4	5.8	-0.7	-0.1	-5.5	-12 3	-20 I	-25.5	
Dew pt.	18.2	14.4	6.0	-0.8	-0.6				-25.5			-32.5	
R.H.	87	79	43	28	36	45	40	21	19	21	49	52	
				20	30	7,5	70	~ 1	12	2. 1	7,	22	
Mix Ratio	13.1	10.9	6.09	3.86	4.10	3.01	1.91	1.04	.70	.51	1.14	1.17	
Sat. V.P.	24.0	20.9	22.0	20.9	16.4	9.2	5.8	6.0	4.1	2.4	1.2	0.8	
V. Press.	20.9	16.4	9.2	5.8	6.0	4.1	2.4	1.2	0.8	0.5	0.6	0.4	
W. Bulb							-						
Temp	19.0	15.9	11.7	8.8	7.1	1.2	-4.7	-5.9	-10.2	-15.7	-22.1	-27.4	
Pot. W.B.													
Temp		17.8	13.7	11.4	10.9	9.0	7.7	8.4	8.2	8.7	23.9	31.1	
Equiv. Pot		54.0											
Temp	56.7	54.2	41.3	34.8	33.5	28.9	25.8	27.3	26.9	28.0	78.6	120.3	
LCL at	Tam	17 9	Press	093	Ho I	ght 26	50						
LOL UI	TOMP.	17.5	11633	. ,0,	1101	9111 20	50						
Mixing L	ayer		(CCL		Conve	ective	Temp		Mean	Mixino	Ratio	
9												,	
Press	Height	P	ress	Heig	gh t								
000	215	0	7.1	701									
988	215		31	725			23.4				12.64		
963	437		28	757			23.1				12.19		
938	662		11	908			22.3				10.68	4	
913	890		82	1173			8.15				8.95		
888 863	1359		63	1361			21.4				7.86		
838			47	1511			21.1				7.08		
813	1602 1846		32 17	1660 1807			0.12				6.47		
7 8 8	2099		03	1007			21.0				5.95		
763	2358		90	2075			21.0				5.50		
,05	2000	,		2012		4	-1.0				2.00		

Units: temperature C; pressure millibar; mixing ratio grams/kilogram; height meters.

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APPENDIX A
PROGRAM LISTING

SCALAR IN ALL FUN EXCEPT Z AND CCL COEITOS, TS, PS) IS POTENTIAL EQUIVALENT/PSEUDO EQUIVALENT TEMP CTHE FOLLOWING SUBROUTINES APPROXIMATE A THERMODYNAMIC CHART SATURATION VAPOR PRESSURE OVER WATER AT TEMP X , Y COORDINATES OF T , P ON SKEWT IN INCHES THICKNESS IN METERS FROM P(1) TO PT CTSA (OS.P) TEMP ON SATURATED ADIABAT OS AT LEVEL CSOUNDINGS MUST BE ORDERED BY DECREASING PRESSURE CCCL (PM, P, T, TD, WBAR, N) IS THE PRESSURE AT THE CCL 01710 CALCL(TOS,TS,PS) IS THE PRESSURE AT THE LCL DITTO CTMR(4,P) TEMP ON MIXING RATIO W AT LEVEL TEMP ON DRY ADIABAT O AT LEVEL CWIT, P) THE MIXING RATIO LINE THROUGH T,P INPUT PRESS AT TOP OF MIXING LAYER CTHERMODYNAMIC CHART SOFTWARE PACKAGE COW(TOS, TS, PS) IS POTENTIAL WET BULB COSITIPI THE SAT ADIABAT THROUGH TIP COIT,P) THE DRY ADIABAT THROUGH T.P CONVECTIVE TEMP CTDS.TS,PS ARE TD.T.P AT SURFACE CN IS NO OF LEVELS IN SOUNDING CHBAR IS THE MEAN MIXING RATIO CT IS TEMPERATURE IN KELVIN. CTE(TOS,TS.PS) IS EQUIV TEMP CT#(TOS,TS,PS) WET BULB TEMP CFR(T,TD) RELATIVE HUMIDITY CP IS PRESSURE IN MILLIBARS CPC 1S PRESSURE AT CCL CO IS REALLY A THETA CTD IS DEWPOINT TEMP DITTO (MBAR, PC, PS) CZ(PT.P.T.TD.N) CTDA(O,P) CESAT(T) CXX(T.P) CYY(P) PAGE CCT FAU

10

-273-16 +273-16 +273.16 ARGUMENTS AND DE (KELVIN) ALL ARGUMENTS AND OS (KELVIN) FUNCTION DE(TOS, TS, PS) TW(TDS,TS,PS) 05(ATW, 1000.) OW(TOS, TS, PS) ATM = TW(TDS, TS, PS) - TSA(A0S,1000.) AOS . OSTATHOPS) FUNCTION ATA END 30 30 RETURN RETURN ALL

SKEN-T PROGRAN ROUTINES

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FUNCTION TE(TDS,TS,PS)
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TE = TDA(AOE,PS)
RETURN

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UU

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ST LEVEL BELOW PH. GRAMS VAPOR/KILOGRM		/P(L))+WBAR
FUNCTION ALCL(TDS,TS,PS) ABS IS ABSOLUTE VALUE ALL ARGUMENTS AND TW (KELVIN) AW = W(TDS,PS) AN = W(TS,PS) AN = W(TS,PS) AN = W(TS,PS) ALCL = PI RETURN END N IS NO. OF LEVELS IN SOUNDING. K IS THE CCL AND P (MILLIBAR) TO KELVIN), WBARAIR.) DIMENSION T(N),P(N),TD(N) WBAR = O K*O K**C	PM) 201,201,200 -LT.1) GO TO 101 AVERAGE MIXING RATIO. ALOG IS LOG	L=1+1 #BAR=(#(TD(1),P(1))+#(TD(L),P(L)))+ALOG(P(1)/P(L))+#BAR
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A2 = T(I)*(1. + .0076078*W(TD(I),F(E)))

Z = Z*I**6*Z85*(AI**Z*)*(ALOG(P(I))/P(J))
                                                                                                                                                                                                                                                                                                                                 z = T(1)*(1 + 0006078*W(TD(1),P(1)))

z = z+14.64285*(A1+A2)*(ALO6(P(1),P(1)))
                                                                                                                                                                                                                                                                                                                  AI = T(J)*(1. + .0006078*W(TD(J),P(J)))
                                                                                                                               DIMENSION T( N), P( N), TD( N)
DIMENSION P(50), T(50), TD(50)
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